# Local Problems on Trees from the Perspectives of Distributed Algorithms, Finitary Factors, and Descriptive Combinatorics

S. Brandt, Y. Chang, J. Grebík, C. Grunau, V. Rozhoň, Z. Vidnyászky



### Summary

In computer science, we study *distributed algorithms* using **LOCAL** model of computing.

In *descriptive combinatorics*, mathematicians study certain "local" constructions.

There are some pretty cool connections between the two fields! [Bernshteyn]

## The LOCAL model of distributed graph algorithms

- Undirected graph on *n* nodes, one computer in each node
- Synchronous message passing rounds, unbounded message size and computation
- Initially, nodes know only (upper bound on) *n*, in the end, each node should know its part of output
- Time complexity: number of rounds
- This talk: the graph is a  $\Delta$ -regular tree with  $\Delta$  constant



LOCAL model [Linial FOCS'87]



# A lot is known! [Many papers in past 10 years]





#### **Descriptive Combinatorics - Circle Squaring**

Can you do this?



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Can you do this?



...Yes! [Laczkovich, Grabowski et al., MarksUnger, Mathé et al., ...]



Main point of the paper:

we try to do the same as in complexity theory, i.e., define lots of complexity classes and prove some inclusions



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Also:

. . .

- introduce the ID graph trick,
- new LOCAL & BOREL lower bounds by generalization of Marks' technique

#### It seems there is a lot things waiting to be discovered!



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